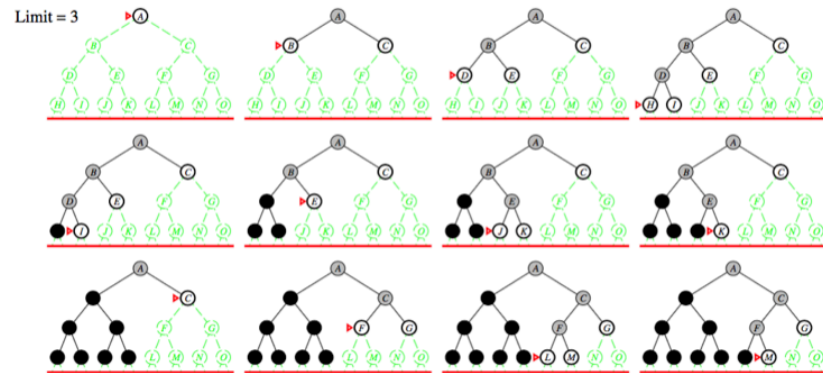
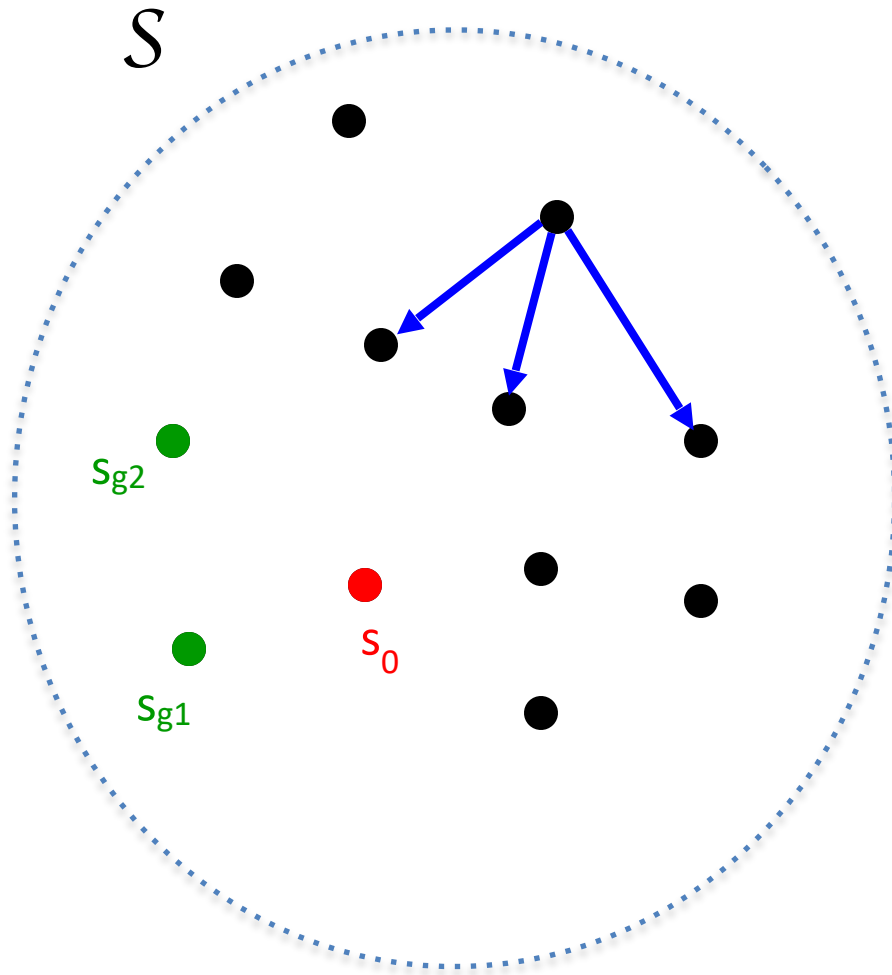


# CS143: Artificial Intelligence



Iterative Deepening Search (IDS)  
BFS and DFS implementation issues

# Recap: abstraction to define a search problem

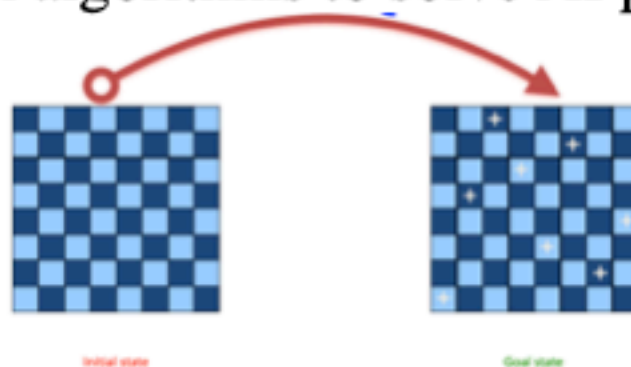


- State space  $S$
- Initial state  $s_0$
- Successor function:  
 $x \in S \rightarrow \text{succ}(s)$ : that encodes possible transitions of the system from state  $s$  to another state  $x$
- Set of goal states:  
 $x \in S \rightarrow \text{GOAL?}(x) = \text{T or F}$
- Cost: that calculates how “expensive” a given set of moves is

# Recap: Abstraction for Old Puzzle



Search algorithms to solve AI problems



State space:

Initial state:

Goal state:

Successor function:

Cost:

# Recap: Concrete Instantiation: Search Algorithm #1

1. If **goal-state** == **initial-state** then return **initial-state**
2. INSERT(**initial-state**, **frontier**)
3. repeat:
4. If empty(**frontier**) then return **failure**
5.  $s \leftarrow$  REMOVE(**frontier**)
6. for every state  $s'$  in SUCC( $s$ ):
7. If **goal-state** ==  $s'$  then return  $s'$  and/or path
8. INSERT( $s'$ , **frontier**)

Expansion of  $s$



# Recap: Search Strategy

- **frontier** is a data structure with two operations:
  - INSERT(node, **frontier**)
  - REMOVE(**frontier**)
- Surprisingly, this algorithm supports many different search strategies depending on implementation of **frontier**
  - yet another example of the power of abstraction

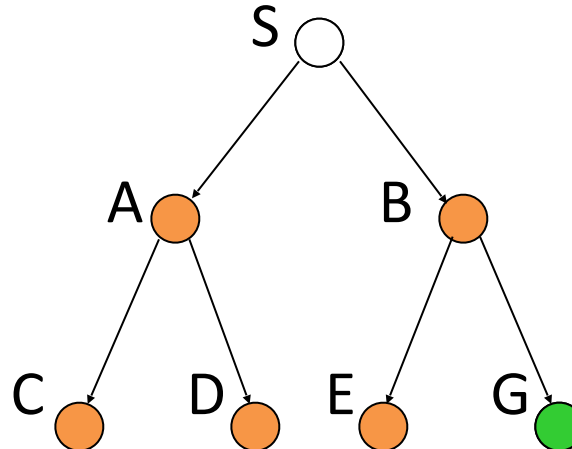
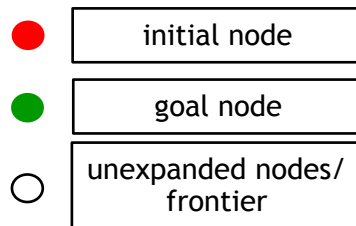
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on **opposite sides** of **frontier**

Queue (frontier):



append: S



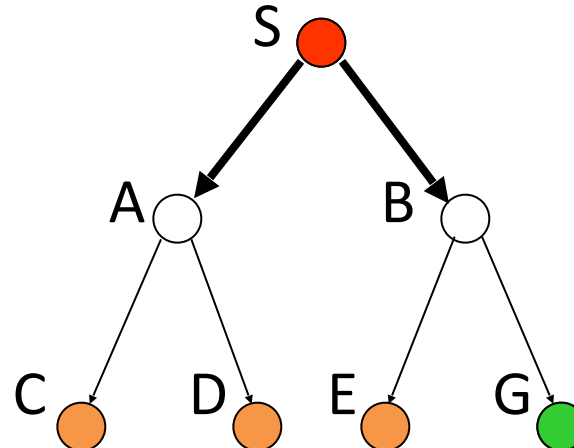
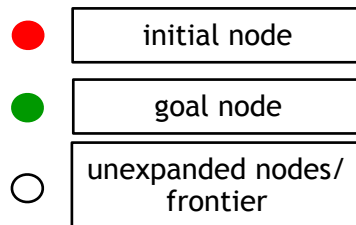
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on **opposite sides** of **frontier**

Queue (frontier):



remove: S  
append: A, B



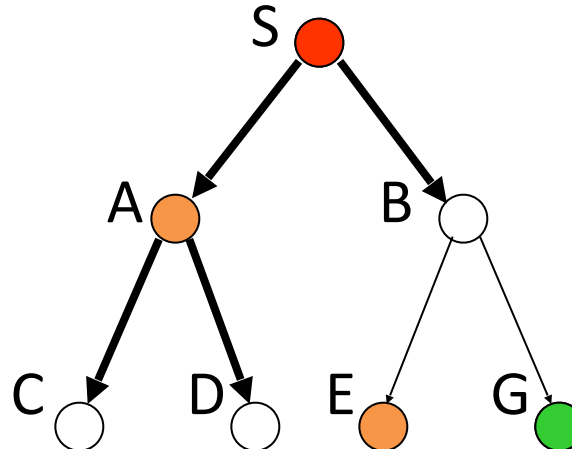
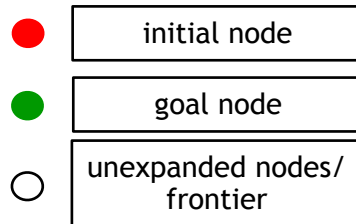
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on **opposite sides** of **frontier**

Queue (frontier):



remove: A  
append: C, D



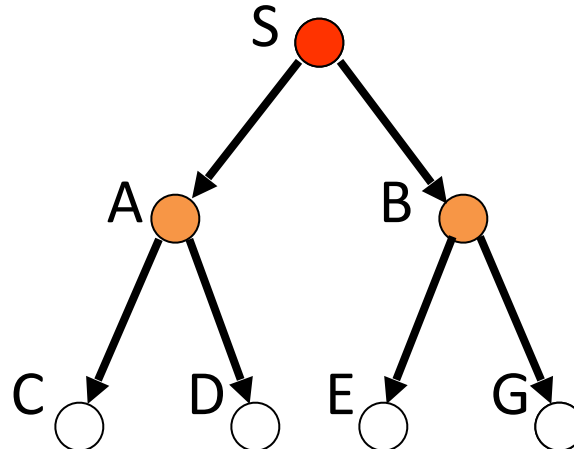
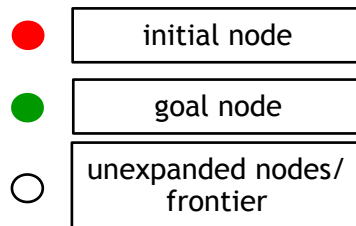
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on **opposite sides** of **frontier**

Queue (frontier):



remove: B  
append: E, G



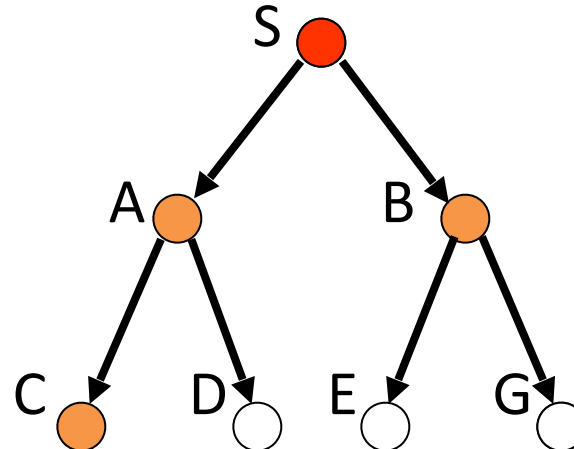
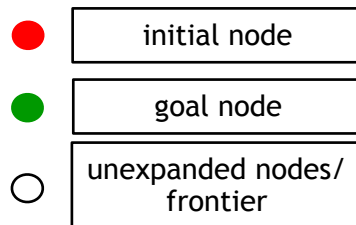
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on opposite sides of **frontier**

Queue (frontier):



remove: C



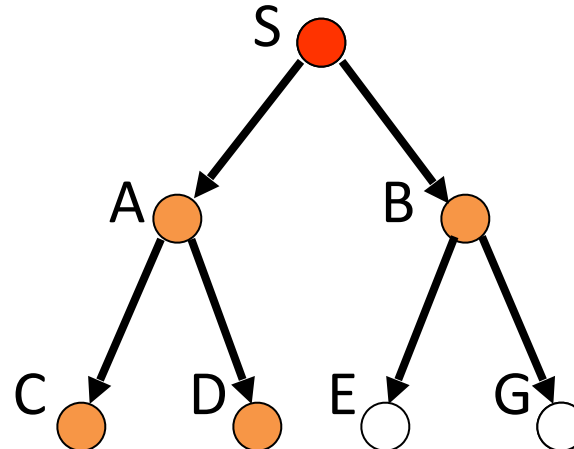
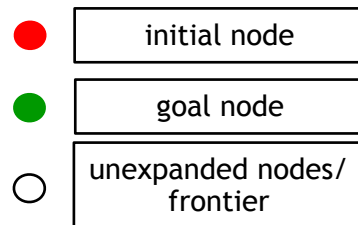
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on **opposite sides** of **frontier**

Queue (frontier):



remove: D



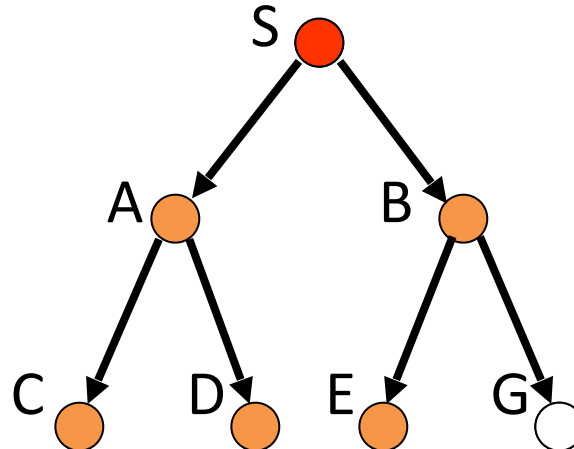
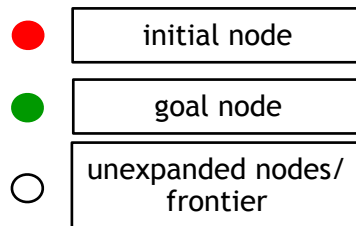
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on opposite sides of **frontier**

Queue (frontier):



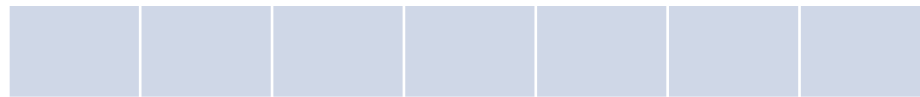
remove: E



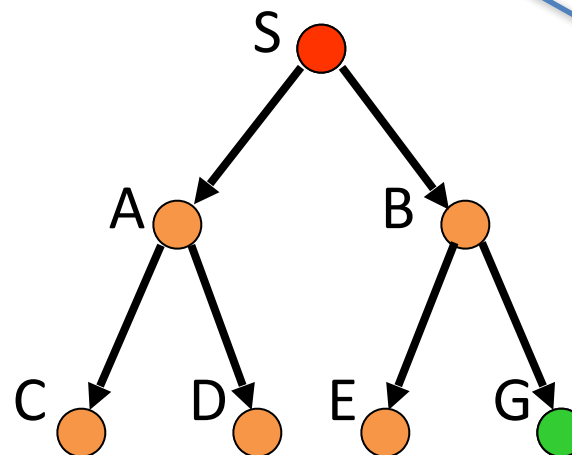
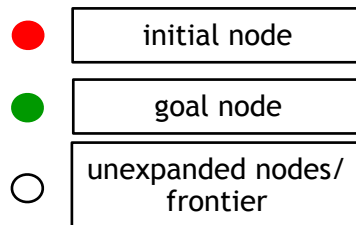
# Illustrating Breadth-First Search (BFS) Algorithm

- Nodes are inserted & removed on opposite sides of **frontier**

Queue (frontier):



remove: G



Reached goal state G  
BFS stops

FRONTIER may or may  
not be empty

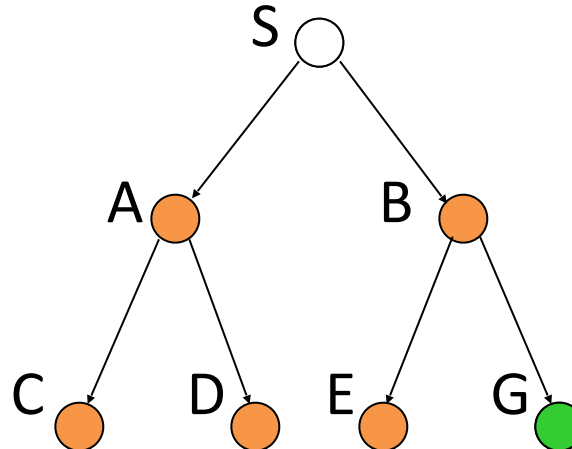
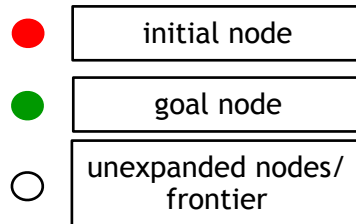
# Recap: Illustrating Depth-First Search (DFS)

- Nodes are inserted & removed on **same sides** of **frontier**

Stack (frontier):



append: S



Thin black edges meant those have not been visited during search

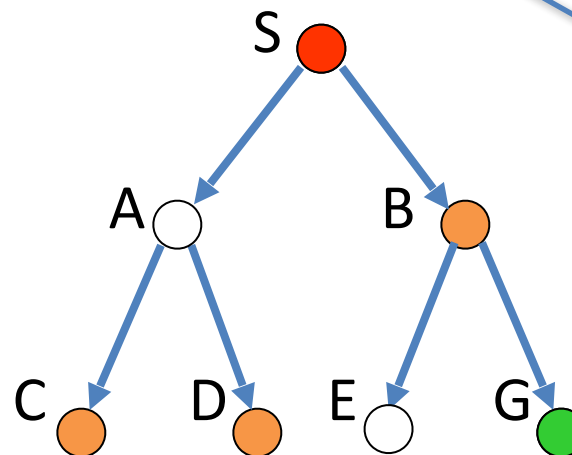
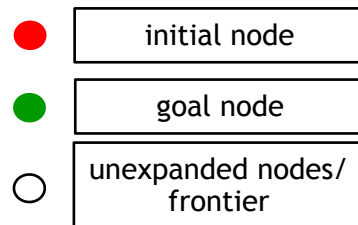
# Recap: Illustrating Depth-First Search (DFS)

- Nodes are inserted & removed on **same sides** of **frontier**

Stack (frontier):



remove: G



Reached goal state G  
DFS stops

FRONTIER may or may not be empty. In this case, it's not empty (A and E)

Blue edges meant those have been visited during search

# Recap: Useful Data Structure in Python: deque

- `deque` is a “double-ended” queue.
  - Reference: <https://docs.python.org/2/library/collections.html#collections.deque>
- Useful methods in `deque`

**`append(x)`**

Add `x` to the right side of the deque.

**`appendleft(x)`**

Add `x` to the left side of the deque.

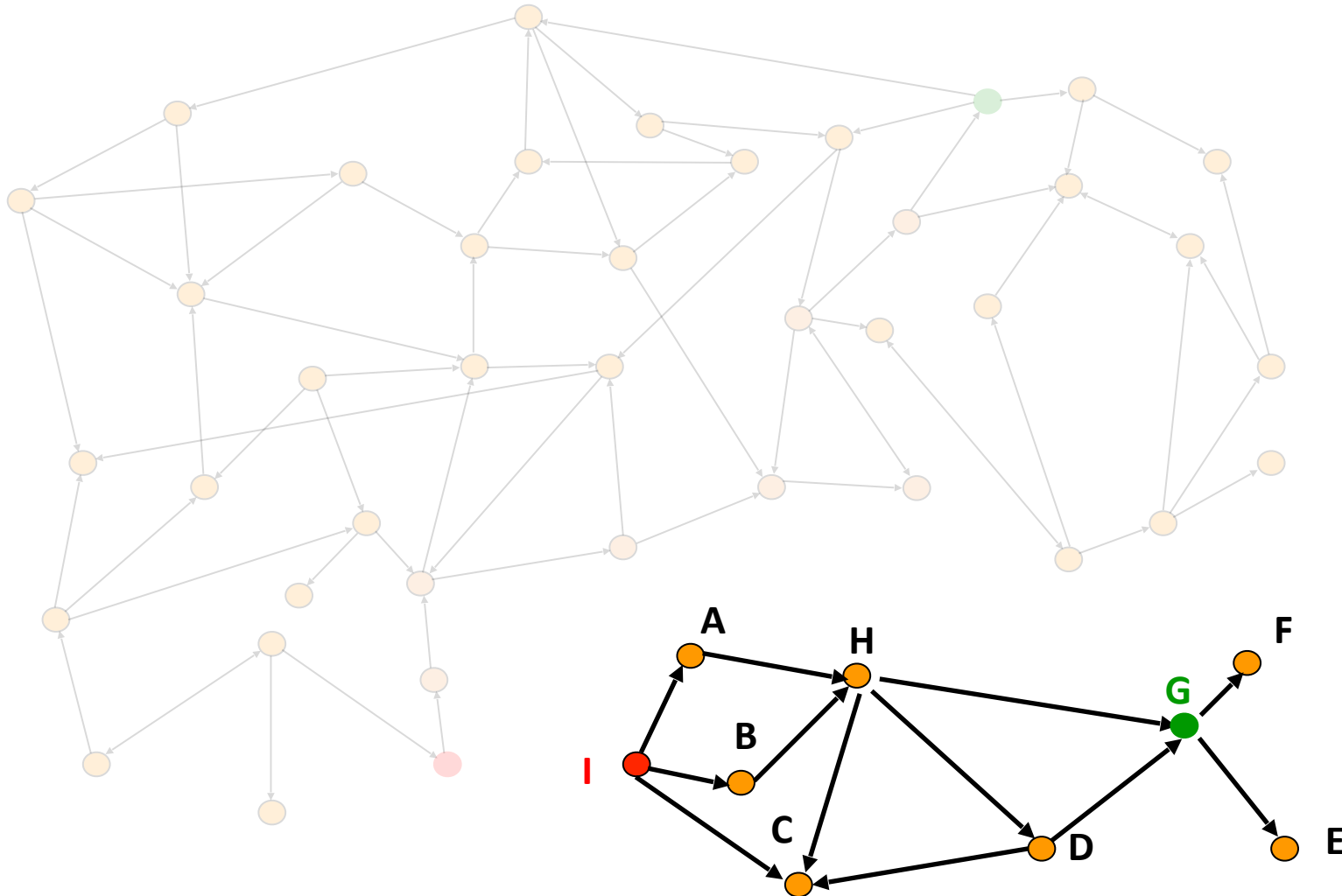
**`pop()`**

Remove and return an element from the right side of the deque

**`popleft()`**

Remove and return an element from the left side of the deque.

# Exercise: Breadth-First Search on the following Graph



# Recap: Useful Data Structure in Python: deque

## Group exercise#1:

Implement the BFS traversal on this `frontier` datastructure.

```
▶ frontier = deque([])
my_list = ['a', 'b', 'c', 'd', 'e']
for i in range(len(my_list)):
    item = my_list[i]
    frontier.append(item)
    print(my_list[0:i+1])

# your code ...
print('BFS traversal ...')
while len(frontier) > 0:
    print("item:", frontier.popleft())
```

```
... ['a']
    ['a', 'b']
    ['a', 'b', 'c']
    ['a', 'b', 'c', 'd']
    ['a', 'b', 'c', 'd', 'e']
    BFS traversal ...
    item: a
    item: b
    item: c
    item: d
    item: e
```

## Group exercise#2:

Implement the DFS traversal on this `frontier` datastructure.

```
▶ frontier = deque([])
my_list = ['a', 'b', 'c', 'd', 'e']
for i in range(len(my_list)):
    item = my_list[i]
    frontier.append(item)
    print(my_list[0:i+1])

# your code ...
print('DFS traversal ...')
while len(frontier) > 0:
    print("item:", frontier.pop())
```

```
... ['a']
    ['a', 'b']
    ['a', 'b', 'c']
    ['a', 'b', 'c', 'd']
    ['a', 'b', 'c', 'd', 'e']
    DFS traversal ...
    item: e
    item: d
    item: c
    item: b
    item: a
```

Reza's solution

<https://colab.research.google.com/drive/1qNltbJYWkDfJKHM0kSGR7Z-GgKOwY4y?usp=sharing>

# Iterative Deepening Search (IDS)

# Iterative Deepening Search (IDS) Algorithm

- Uses a limited version of DFS called **depth-limited search**
  - nodes at depth  $l$  has no successors
- do a **depth-limited search** with  $l = 0$ , if it fails,
- do a **depth-limited search** with  $l = 1$ , if it fails,
- do a **depth-limited search** with  $l = 2$ , if it fails,
  - ...
  - ...
  - ...
- until you find a goal

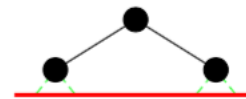
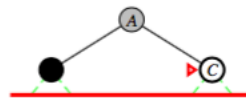
# Iterative Deepening Search (IDS) Algorithm

Limit = 0



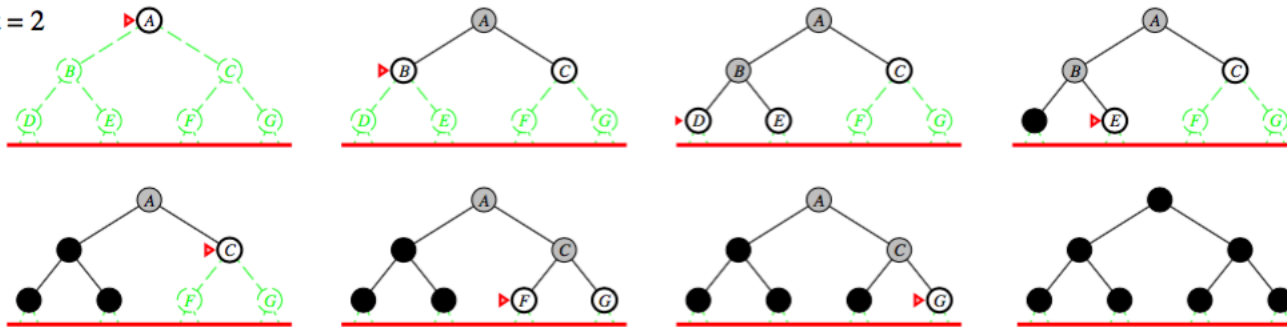
# Iterative Deepening Search (IDS) Algorithm

Limit = 1



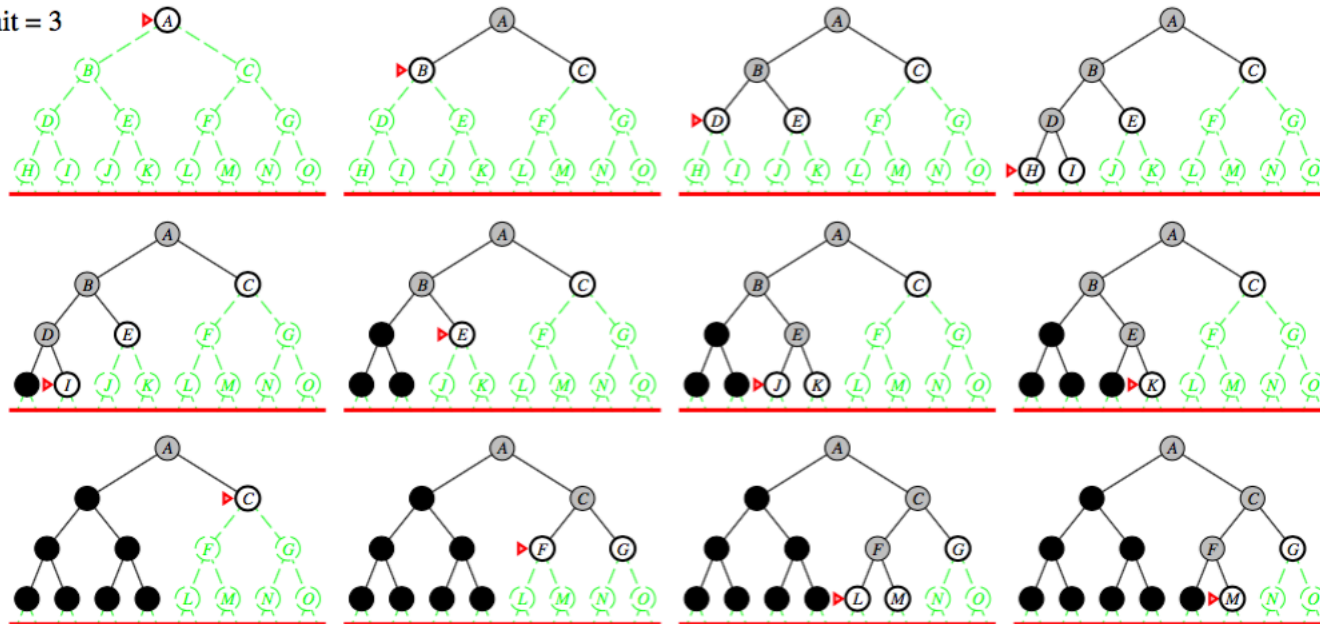
# Iterative Deepening Search (IDS) Algorithm

Limit = 2



# Iterative Deepening Search (IDS) Algorithm

Limit = 3



# Today: Practical Implementation

- Practical implementation of AI problem solving as search
  - Introduce the python code for search
  - Explore the code in-class